

**Law of Sines and the Ambiguous Case - Guided Lesson Explanation:****Explanation#1**

Use the Law of Sines:  $a/\sin A = c/\sin c$

$$8/40^\circ = 17/\sin c$$

$$8(\sin C) = 17 \cdot \sin 40^\circ$$

$$\sin C = 17 \cdot (0.6)/8 = 1.275$$

Since  $\sin C$  must be  $\leq 1$ , no angle exists for angle  $C$ .  
NO triangle exists for these measurements.

**Explanation#2**

Use the Law of Sines:  $a/\sin A = b/\sin B$

$$12/20^\circ = 17/\sin B$$

$$12(\sin B) = 17 \cdot \sin 20^\circ$$

$$\sin B = 17 \cdot (0.3)/12 = 0.425$$

Angles could be  $20^\circ$ ,  $25.15^\circ$ , and  $134.85^\circ$ : sum  $180^\circ$

Now  $m\angle A = 20^\circ$  and  $m\angle B = 25.15^\circ$  the sum of the angles would exceed  $180^\circ$ . Not possible! Therefore,  $m\angle B = 25.15^\circ$ ,  $m\angle A = 20^\circ$ , and  $m\angle C = 134.85^\circ$  and only ONE triangle is possible.

**Explanation#3**

Use the Law of Sines:  $a/\sin A = b/\sin B$

$$15/40^\circ = 20/\sin B$$

$$15(\sin B) = 20 \cdot \sin 40^\circ$$

$$\sin B = 20 \cdot (0.6)/15 = 0.8$$

Angles could be  $40^\circ$ ,  $53.13^\circ$ , and  $86.87^\circ$ , sum  $180^\circ$

Now  $m\angle A = 40^\circ$  and  $m\angle B = 53.13^\circ$  the sum of the angles would exceed  $180^\circ$ . Not possible! Therefore,  $m\angle B = 53.13^\circ$ ,  $m\angle A = 40^\circ$ , and  $m\angle C = 86.87^\circ$  and only ONE triangle is possible.

