

Name \_\_\_\_\_

Date \_\_\_\_\_

## Logarithmic Equations - Guided Lesson Explanation

While solving these questions you should keep the following properties in mind:

$$\log_b m \cdot n = \log_b m + \log_b n \quad \ln ab = \ln a + \ln b$$

$$\log_b m/n = \log_b m - \log_b n \quad \ln a/b = \ln a - \ln b$$

$$\log_b m^r$$

$$= r \log_b m \quad \ln a^b$$

$$= b \ln a$$

### Explanation#1

Isolate the logarithmic expression first

$$14 + 6 \ln x = 20$$

$$6 \ln x = 20 - 14$$

$$6 \ln x = 6$$

$$\ln x = \frac{6}{6}$$

$$\ln x = 1$$

Remember that  $e^x$

and  $\ln x$  are inverse functions.

$$e^{\ln x}$$

$$= e^3$$

Hence,

$$x = e^3$$

$$(e \ln x$$

$$= x)$$

So the answer is  $x = e^3$



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### **Explanation#2**

**Isolate the logarithmic expression first**

$$12 + 4\ln x = 4$$

$$4\ln x = 4 - 12$$

$$4\ln x = -8$$

$$\ln x = \frac{-8}{4}$$

$$\ln x = -2$$

**Remember that  $e^x$  and  $\ln x$  are inverse functions.**

$$e^{\ln x} = e^{-2}; x = e^{-2} \quad (e^{\ln x} = x)$$

**So the answer is  $x = e^{-2}$**

### **Explanation#3**

**Isolate the logarithmic expression first**

$$3 + 2\ln x = 13$$

$$2\ln x = 13 - 3$$

$$2\ln x = 10$$

$$\ln x = \frac{10}{2}$$

$$\ln x = 5$$

**Remember that  $e^x$  and  $\ln x$  are inverse functions.**

$$e^{\ln x} = e^5; x = e^5 \quad (e^{\ln x} = x)$$

**So the answer is  $x = e^5$**

