Solving Quadratic Equations - Guided Lesson Explanation

The quadratic equation is stated as:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Explanation #1

Solving by factoring:

$$x^{2} + 5x - 20 = 16$$

 $x^{2} + 5x - 36$ (Combine Like Terms)
 $(x + 9) (x - 4)$ (Factor)
 $x + 9 = 0$ $x - 4 = 0$ (solve for x)
 $x = -9$ $x = 4$

Solving by using the quadratic equation:

Step 1) Place the numbers into the formula:

$$x = \frac{-5 \pm \sqrt{5^2 - 4 \times 1 \times (-36)}}{2 \times 1} \qquad x = \frac{-5 \pm \sqrt{169}}{2}$$
 Step 2) Calculate.

Step 3) Finalize by calculating both the plus and minus version.

$$x_1 = \frac{-5 + \sqrt{169}}{2} = 4$$

$$x_2 = \frac{-5 - \sqrt{169}}{2} = -9$$

Explanation #2

$$x^2 - 6x - 18 = 9$$

$$x^2 - 6x - 27$$

 x^2 - 6x - 27 (Combine Like Terms)

$$(x + 9)(x - 3)$$

(Factor)



$$x + 9 = 0$$

$$x + 9 = 0$$
 $x - 3 = 0$ (Solve for x)

$$x = -9$$
 $x = 3$

$$x = 3$$

Solving by using the quadratic equation:

Step 1) Place the numbers into the formula:

$$x = \frac{-6 \pm \sqrt{6^2 - 4 \times 1 \times (-27)}}{2 \times 1}$$

Step 2) Perform all the operations.

$$x = \frac{-6 \pm \sqrt{144}}{2}$$

Step 3) Finalize by calculating both the plus and minus version.

$$x_1 = \frac{-6 + \sqrt{144}}{2} = 3$$

$$x_2 {=} \frac{\text{-}6 \ \text{-} \ \sqrt{144}}{2} = \text{-}9$$

Explanation #3

$$x^2 + 4x - 32$$

 $x^2 + 4x - 32$ (No like terms to combine.)

$$(x + 8) (x - 4)$$
 (Factor)





$$x + 8 = 0$$

$$x - 4 = 0$$

$$x + 8 = 0$$
 $x - 4 = 0$ (Solve for x)

$$x = -8$$
 $x = 4$

$$x = 4$$

Solving by using the quadratic equation:

Step 1) Place the numbers into the formula:

$$x = \frac{-4 \pm \sqrt{4^2 - 4 \times 1 \times (-32)}}{2 \times 1}$$

Step 2) Perform all the operations.

$$x = \frac{-4 \pm \sqrt{144}}{2}$$

Step 3) Finalize by calculating with both plus and minus version.

$$x_1 {=} \frac{\text{-}4 \ + \sqrt{144}}{2} = \ 4$$

$$x_2 {=} \frac{\text{-}4 \, \cdot \, \sqrt{144}}{2} = \, \text{-}8$$