

**Cavalieri's Principle - Independent Practice Worksheet**

Complete all the problems. Make sure to draw pictures to help you solve the problems.

1. Calculate the volume of the "globe" with circular cross-sectional area equal to  $\pi \sqrt[12]{x^4}$  above  $x$  in the interval  $[0, 1]$ .
2. Calculate the volume of the "ball" with circular cross-sectional area equal to  $\pi \sqrt[6]{x^8}$  above  $x$  in the interval  $[0, 1]$ .
3. Calculate the volume of the "egg" with circular cross-sectional area equal to  $\pi \sqrt[14]{x^3}$  above  $x$  in the interval  $[0, 1]$ .
4. Calculate the volume of the "lemon" with circular cross-sectional area equal to  $\pi \sqrt[18]{x^4}$  above  $x$  in the interval  $[0, 1]$ .
5. Calculate the volume of the "coin" with circular cross-sectional area equal to  $\pi \sqrt[8]{x^5}$  above  $x$  in the interval  $[0, 1]$ .
6. Let  $A(x) = \sqrt[12]{x^3}$  describes the area of a cross-section of a block at  $x$  (perpendicular to the  $x$ -axis). Find the volume of block from  $x=0$  to  $x=1$ .
7. Let  $A(x) = \sqrt[5]{x^9}$  describes the area of a cross-section of a stone at  $x$  (perpendicular to the  $x$ -axis). Find the volume of stone from  $x=0$  to  $x=1$ .
8. Let  $A(x) = \sqrt[10]{x^4}$  describes the area of a cross-section of a brick at  $x$  (perpendicular to the  $x$ -axis). Find the volume of brick from  $x=0$  to  $x=1$ .
9. Let  $A(x) = \sqrt[11]{x^6}$  describes the area of a cross-section of a ice at  $x$  (perpendicular to the  $x$ -axis). Find the volume of ice from  $x=0$  to  $x=1$ .
10. Let  $A(x) = \sqrt[9]{x^{11}}$  describes the area of a cross-section of a cake at  $x$  (perpendicular to the  $x$ -axis). Find the volume of cake from  $x=0$  to  $x=1$ .

