

Name _____

Date _____

Using Sine and Cosine - Step-by-Step Lesson

Use the Law of Sine and the Law of Cosine to find the missing sides and angles of each triangle.

$BC = 12$, $\angle B = 42^\circ$, and $\angle C = 30^\circ$

Explanation:

We need to find 1) angle A 2) length of AC 3) length of AB

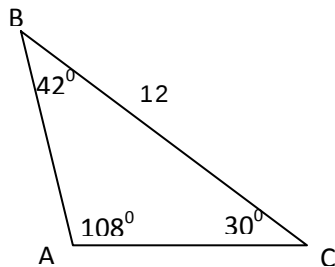
Start with the missing angle:

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 42^\circ + 30^\circ = 180^\circ$$

$$\angle A + 72^\circ = 180^\circ \text{ (Subtract } 72^\circ \text{ from both sides)}$$

$$\angle A = 108^\circ$$



The law of sin is based on the proportionality of side and angle in triangle. The law states that for the angle of a non right angle, each angle of the triangle has the same ratio of angle measure to sine value.

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

Substitute the known value into the law of Sine to find AB.



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$$\frac{\sin(30)}{c} = \frac{\sin(108)}{12}$$

Solve the equation for AC

$$AB = c = 6.31$$

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$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

Substitute the known value into the law of sin to find AC.

$$\frac{\sin(108)}{12} = \frac{\sin(42)}{AC}$$

Solve the equation for AC

$$AC = b = 8.44$$

