

Symmetry of the Unit Circle and Odd-Even Properties - Guided Lesson Explanation**Explanation#1**

The sine function $f(t) = \sin t$ is odd and the cosine function $g(t) = \cos t$ is even; that is, for every real number t ,

$$\sin\left(-\frac{\pi}{3}\right) = -\sin\frac{\pi}{3} = -\frac{\sqrt{3}}{2}$$

$$\cos\left(-\frac{\pi}{3}\right) = \cos\frac{\pi}{3} = \frac{1}{2}$$

Note that the signs of the answers are consistent with the fact that the terminal side of the angle $-\pi/3$ radian lies in quadrant IV.

Explanation#2

The sine function $f(t) = \sin t$ is odd and the cosine function $g(t) = \cos t$ is even; that is, for every real number t ,

$$\sin\left(-\frac{2\pi}{3}\right) = -\sin\frac{2\pi}{3} = -\frac{\sqrt{3}}{2}$$

$$\cos\left(-\frac{2\pi}{3}\right) = \cos\frac{2\pi}{3} = -\frac{1}{2}$$

Note that the signs of the answers are consistent with the fact that the terminal side of the angle $-2\pi/3$ radian lies in quadrant III.

Explanation#3

The sine function $f(t) = \sin t$ is odd and the cosine function $g(t) = \cos t$ is even; that is, for every real number t ,

$$\sin\left(-\frac{3\pi}{4}\right) = -\sin\frac{3\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\cos\left(-\frac{3\pi}{4}\right) = \cos\frac{3\pi}{4} = -\frac{\sqrt{2}}{2}$$

Note that the signs of the answers are consistent with the fact that the terminal side of the angle $-3\pi/4$ radian lies in quadrant III.

