

BINOMIAL THEOREM FOR EXPANSION



Binomial Theorem for Expansion is used to expand the powers of a binomial expression.

Formula of binomial expansion is:

$$(1 + x)^n = \sum_{k=0}^n \binom{n}{k} x^k$$

Example

$$(a+b)^2 = a^2 + 2ab + b^2$$

Using Binomial Theorem for Expansion

EXAMPLE

$$\text{EXPAND } (3x-4)^3$$

$$\text{WE KNOW THAT: } (a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3 \quad \text{Using Binomial Theorem of Expansion}$$

$$\text{Putting } a=3x \text{ and } b=-4$$

$$\begin{aligned} \text{So, } (3x-4)^3 &= (3x)^3 + 3(3x)^2(-4) + 3(3x)(-4)^2 + (-4)^3 && \text{Putting } a=3x \text{ and } b=-4 \\ &= (3^3 \cdot x^3) + 3(3^2 \cdot x^2)(-4) + 3(3x)(16) + (-64) && \text{Using } (ab)^2 = a^2 \cdot b^2 \\ &= 27x^3 + 3(9x^2)(-4) + (144x) - 64 \\ &= 27x^3 - 108x^2 + 144x - 64 \\ &= 27x^3 - 108x^2 + 144x - 64 \end{aligned}$$

Meets: Common Core Standard High School – HSA-APR.C.5