

Quadratic Equations: Completing the Square - Guided Lesson Explanation

For the problems we can complete the square by adding $\left(\frac{b}{2}\right)^2$ with quadratic expressions like $x^2 + bx$.

Explanation#1

Now we will add $\left(\frac{b}{2}\right)^2$ to complete the square.

$$\begin{aligned} & t^2 + 16t + \left(\frac{b}{2}\right)^2 \\ &= t^2 + 16t + \left(\frac{16}{2}\right)^2 \\ &= t^2 + 16t + (8)^2 \\ &= t^2 + 16t + 64 \end{aligned}$$

So, this quadratic can be written as a square, $(t + 8)^2$, and therefore it is a perfect-square quadratic.

So, the number needed to complete the square was 64.

Explanation#2

Now we will add $\left(\frac{b}{2}\right)^2$ to complete the square.

$$\begin{aligned} & t^2 + 26t + \left(\frac{b}{2}\right)^2 \\ &= t^2 + 26t + \left(\frac{26}{2}\right)^2 \\ &= t^2 + 26t + (13)^2 \\ &= t^2 + 26t + 169 \end{aligned}$$

So, this quadratic can be written as a square, $(t + 13)^2$, and therefore it is a perfect-square quadratic.

So, the number needed to complete the square was 169.



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Explanation#3

Now we will add $(\frac{b}{2})^2$ to complete the square.

$$\begin{aligned} & t^2 + 18t + (\frac{b}{2})^2 \\ &= t^2 + 18t + (\frac{18}{2})^2 \\ &= t^2 + 18t + (9)^2 \\ &= t^2 + 18t + 81 \end{aligned}$$

So, this quadratic can be written as a square, $(t + 9)^2$, and therefore it is a perfect-square quadratic.

So, the number needed to complete the square was 81.

