

**Proving Polynomial Identities - Guided Lesson Explanation**

**For all the problems in this section, we know that the square of a binomial is:**

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

**Explanation#1**

We can see that  $(3x + 4y)^2$  is the square of a binomial just like

$(a + b)^2$ . So, we will find  $(3x + 4y)^2$  with this formula.

$$(a + b)^2 = a^2 + 2ab + b^2$$

We will replace (a) with 3x and (b) with 4y, then solve.

$$\begin{aligned} &(3x + 4y)^2 \\ &= (3x)^2 + 2(3x)(4y) + 4y^2 \\ &= 9x^2 + 24xy + 16y^2 \end{aligned}$$

**Explanation#2**

We can see that  $\left(\frac{x}{2} - \frac{y}{3}\right)^2$  is the square of a binomial just like

$(a - b)^2$ . So, we will find  $\left(\frac{x}{2} - \frac{y}{3}\right)^2$  with this formula.

$$(a - b)^2 = a^2 - 2ab + b^2$$

We will replace (a) with  $\frac{x}{2}$  and (b) with  $\frac{y}{3}$ , then solve.

$$\begin{aligned} &\left(\frac{x}{2} - \frac{y}{3}\right)^2 \\ &= \left(\frac{x}{2}\right)^2 - 2\left(\frac{x}{2}\right)\left(\frac{y}{3}\right) + \left(\frac{y}{3}\right)^2 \\ &= \frac{x^2}{4} - \frac{1}{3}xy + \frac{y^2}{9} \end{aligned}$$



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### Explanation#3

We can see that  $(6g + 2h)^2$  is the square of a binomial just like

$(a + b)^2$ . So, we will find  $(6g + 2h)^2$  with this formula.

$$(a + b)^2 = a^2 + 2ab + b^2$$

We will replace (a) with 6g and (b) with 2h, then solve.

$$\begin{aligned} & (6g + 2h)^2 \\ &= (6g)^2 + 2(6g)(2h) + 2h^2 \\ &= 36g^2 + 24gh + 4h^2 \quad \text{Divide everything by 4 to get in simplest form.} \\ &= 9g^2 + 6gh + h^2 \end{aligned}$$

