

# APPLYING THE REMAINDER THEOREM

The Remainder Theorem is a theorem in algebra which states that if  $f(x)$  is a polynomial in  $x$  and  $f(x)$  is divided by  $x-c$  then the remainder is  $f(c)$ .

*Example*

If  $2x^2-4x+3$  is divided by  $x-2$  then the remainder is  $f(2)$ .

## APPLYING THE REMAINDER THEOREM

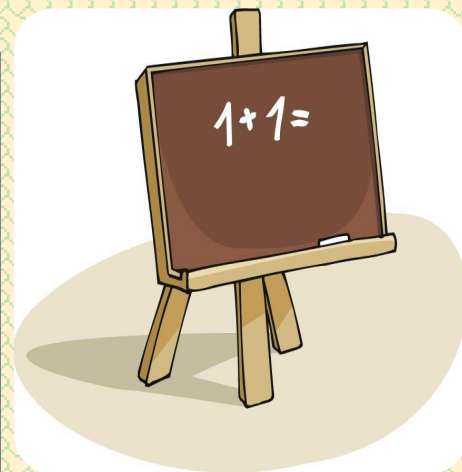
IF  $F(X) = 3X^2-4X+5$  IS DIVIDED BY  $X+2$  THEN:

$$\begin{aligned} \text{REMAINDER} &= F(-2) = 3(-2)^2-4(-2)+5 && \text{PUTTING } X=-2 \text{ IN ALL TERMS} \\ &= 3(4)-(-8)+5 && \text{ADDING OR SUBTRACTING TERMS} \\ &= 12+8+5 = 25 && \text{RESULT IS REMAINDER} \end{aligned}$$

IF  $-2X^3+4X^2-5X+6$  IS DIVIDED BY  $2X-3$  THEN:

$$F(X) = -2X^3+4X^2-5X+6$$

$$\begin{aligned} \text{REMAINDER} &= F\left(\frac{3}{2}\right) \\ &= -2\left(\frac{3}{2}\right)^3+4\left(\frac{3}{2}\right)^2-5\left(\frac{3}{2}\right)+6 && \text{PUTTING } X=3/2 \text{ IN ALL TERMS} \\ &= -2\left(\frac{3^3}{2^3}\right)+4\left(\frac{3^2}{2^2}\right)-5\left(\frac{3}{2}\right)+6 && \text{USING } \left(\frac{a}{b}\right)^2 = \frac{a^2}{b^2} \\ &= -2\left(\frac{27}{8}\right)+4\left(\frac{9}{4}\right)-5\left(\frac{3}{2}\right)+6 \\ &= -\frac{54}{8} + \frac{36}{4} - \frac{15}{2} + 6 && \text{MULTIPLYING FRACTIONS WITH INTEGERS} \\ &= \frac{-54+36(2)-15(4)+6(8)}{8} = \frac{-54+72-60+48}{8} = \frac{6}{8} = \frac{3}{4} && \text{TAKING LCM} \end{aligned}$$



**Meets: Common Core Standard High School – HSA-APR.B.2**